

**WELSH JOINT EDUCATION COMMITTEE**

**CYD-BWYLLGOR ADDYSG CYMRU**

**General Certificate of Education**

**Tystysgrif Addysg Gyffredinol**

**Advanced Level/Advanced Subsidiary**

**Safon Uwch/Uwch Gyfrannol**

**MATHEMATICS M2**

**Mechanics**

**Specimen Paper 2005/2006**

(1  $\frac{1}{2}$  hours)

**INSTRUCTIONS TO CANDIDATES**

Answer **all** questions.

Take  $g$  as  $9.8 \text{ ms}^{-2}$ .

**INFORMATION FOR CANDIDATES**

A calculator may be used for this paper.

A formula booklet is available and may be used.

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

1. At time  $t$  s, the velocity  $v \text{ ms}^{-1}$  of a particle moving on the  $x$ -axis is given by

$$v = 3t^2 + 10t^4.$$

- (a) Find the acceleration of the particle at time  $t$  s. [2]
- (b) Given that when  $t = 0$ ,  $x = -3$ , find the displacement of the particle at time  $t = 2$  s. [4]
2. A vehicle, of mass 8000 kg, is travelling on a straight road. The resistance to motion of the vehicle is constant at 600 N.
- (a) Find the power developed by the vehicle's engine when the road is horizontal and the vehicle is moving at a constant speed of  $25 \text{ ms}^{-1}$ . [3]
- (b) The vehicle now climbs a hill inclined at angle  $\alpha$  to the horizontal, where  $\sin \alpha = \frac{1}{14}$ , with its engine working at a rate of 36 kW. Find the acceleration of the vehicle at the instant when its speed is  $3 \text{ ms}^{-1}$ . [5]
3. A small block, of mass 0.4 kg, lies on a smooth plane inclined at an angle  $\alpha$  to the horizontal, where  $\sin \alpha = \frac{3}{5}$ . The block is attached to one end of a light elastic string of natural length 0.7 m and modulus 19.6 N. The other end of the string is attached to a fixed point A. The block is below the level of A and the string is parallel to a line of greatest slope of the plane. Initially, the block is held with the string extended by 0.5 m.
- (a) Find the initial tension in the string. [2]
- (b) Calculate the initial energy stored in the string. [2]
- The block is now released.
- (c) Calculate the speed of the block when the string just becomes slack. [6]

4. A ball is kicked from a point  $A$  on a horizontal field with an initial speed of  $24.5 \text{ ms}^{-1}$  at an angle of  $30^\circ$  above the horizontal. The ball first hits the ground again at the point  $B$ .
- (a) Calculate the time of flight of the ball. [4]
  - (b) Calculate the distance  $AB$ . [2]
  - (c) Calculate the greatest height reached by the ball. [2]
  - (d) Find the speed and direction of motion of the ball after 2s. [6]
5. A particle moves with constant acceleration. Initially, the particle is moving with velocity  $(\mathbf{i} + 2\mathbf{j}) \text{ ms}^{-1}$ . The velocity of the particle at  $t = 2 \text{ s}$  is  $(3\mathbf{i} - 2\mathbf{j}) \text{ ms}^{-1}$ .
- (a) Show that its acceleration is  $\mathbf{i} - 2\mathbf{j}$ . [2]
  - (b) Find the velocity of the particle at time  $t \text{ s}$ . [4]
  - (c) Determine the time when the velocity vector is perpendicular to the acceleration vector. [3]
  - (d) Given that the initial position vector of the particle is  $(2\mathbf{i} - \mathbf{j})\text{m}$ , find the position vector of the particle at time  $t$ . [4]
  - (e) Evaluate the distance of the particle from the origin at time  $t = 2 \text{ s}$ . [3]
6. A smooth hemispherical bowl, of radius  $a \text{ m}$ , placed upside down and fixed on a horizontal table. A ball bearing, of mass  $m \text{ kg}$ , is placed at  $A$ , the top of the bowl, and projected with a horizontal speed  $u \text{ ms}^{-1}$ . A short time after projection, the ball bearing is still in contact with the bowl at a point  $P$  and moving with speed  $v \text{ ms}^{-1}$ . The point  $O$  is the centre of the circular rim of the bowl and angle  $AOP$  is denoted by  $\theta$ .
- (a) Find an expression for  $v^2$  in terms of  $a$ ,  $g$  and  $\theta$ . [4]
  - (b) Show that the reaction,  $R$ , of the bowl on the ball bearing, is given by
 
$$R = mg(3\cos\theta - 2) - \frac{mu^2}{a}. \quad [5]$$
  - (c) Given that  $a = 0.5$  and  $u = 2$ , calculate the value of  $\theta$  at which the ball bearing leaves the bowl. [3]

7. One end  $A$  of a light inextensible rope  $AB$ , of length  $0.8$  m, is attached to the top of a fixed vertical pole. The other end  $B$  is attached to a small ball of mass  $0.2$  kg. A boy holds the ball so that the rope makes an angle of  $30^\circ$  with the pole. He then hits the ball so that the point  $B$  moves with speed  $u$   $\text{ms}^{-1}$  in a horizontal circle, with the rope remaining at  $30^\circ$  to the vertical throughout the motion.
- (a) Calculate the magnitude of the tension in the rope. [3]
- (b) Find the value of  $u$ , correct to two decimal places. [5]
- (c) What assumption does the word 'light' enable you to make in your solution. [1]