



GCE AS/A level

984/01

MATHEMATICS S2
Statistics 2

A.M. TUESDAY, 15 June 2010

1½ hours

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet;
- a calculator;
- statistical tables (Murdoch and Barnes or RND/WJEC Publications)

INSTRUCTIONS TO CANDIDATES

Answer **all** questions.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

INFORMATION FOR CANDIDATES

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

1. A large batch of tomatoes is delivered to a packing station. The weights of these tomatoes may be assumed to be independent and normally distributed with mean 106 grams and standard deviation 8 grams.

- (a) Find the probability that the weight of a randomly selected tomato exceeds 120 grams. [3]
- (b) A pack contains 10 randomly selected tomatoes. Find the probability that the total weight of these 10 tomatoes is less than 1 kilogram. [6]

2. The number of computer breakdowns per day at a large office may be assumed to follow a Poisson distribution with mean μ . The IT Manager believes that the value of μ should be 1.5 but he decides to check this. He therefore defines the following hypotheses.

$$H_0: \mu = 1.5; \quad H_1: \mu \neq 1.5$$

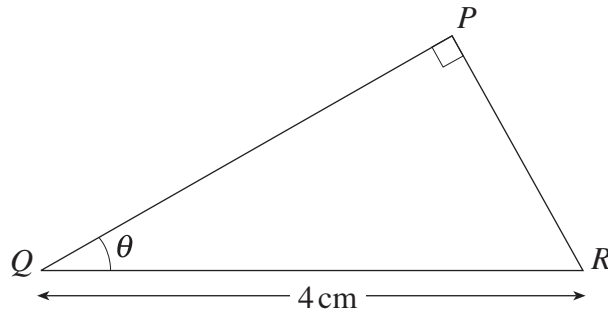
- (a) For one test, he decides to count the number of breakdowns, x , in a 10-day period and to define the critical region as $x \leq 9$ or $x \geq 22$. Find the significance level of this test. [5]
- (b) For another test, he decides to count the number of breakdowns occurring during a 100-day period. Given that 170 breakdowns occur, calculate the approximate p -value and state your conclusion. [7]

3. When a weighing machine is used to weigh an object, the reading obtained, in grams, is a normally distributed random variable with mean equal to the actual weight of the object and standard deviation 0.2. Successive weighings are independent.

- (a) When an object A was weighed three times, the readings obtained were 11.5, 11.7 and 11.6. Calculate a 95% confidence interval for the weight of object A. [5]
- (b) Before an object B was weighed, Graham believed that it would weigh 12 grams but Jim believed that it would weigh more than that.
- (i) State suitable hypotheses to test their beliefs.
- (ii) When the object B was weighed four times, the readings obtained were 12.1, 12.2, 12.4 and 12.1. Calculate the p -value of the four readings and state your conclusion. [7]
- (c) Calculate a 90% confidence interval for the difference between the weights of objects A and B. [5]

4. (a) The random variable X has the binomial distribution $B(n, p)$. Given that $E(X) = 3$ and $E(X^2) = 11.1$, find the values of n and p . [6]
- (b) The independent random variable Y has the binomial distribution $B(15, 0.4)$ and $U = XY$. Find the mean and variance of U . [8]

5.



The above diagram shows a right-angled triangle in which the hypotenuse $QR = 4$ cm and $\widehat{PQR} = \theta$ radians, where θ is a continuous random variable uniformly distributed between 0 and $\frac{\pi}{4}$.

- (a) Show that the area, A cm², of the triangle PQR is given by

$$A = 4 \sin 2\theta. \quad [1]$$

- (b) Calculate $P(A \leq 2)$. [5]

- (c) Determine $E(A)$. [4]

6. Ann and Brenda buy a packet of seeds which states that, on average, 75% of the seeds will germinate. They believe, however, that the germination rate is less than this so they plant a certain number of seeds and count how many germinate.

- (a) State suitable hypotheses. [1]

- (b) Ann plants 50 seeds and decides to reject the statement on the packet if less than 30 germinate.

- (i) Find the significance level of this procedure.

- (ii) Find the probability of accepting the statement on the packet if the actual germination rate is 50%. [6]

- (c) Brenda plants 200 seeds and finds that 140 germinate. Find the approximate p -value of this result and state your conclusion in context. [6]