



GCE MARKING SCHEME

SUMMER 2016

Mathematics – S2
0984/01

INTRODUCTION

This marking scheme was used by WJEC for the Summer 2016 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

GCE Mathematics - S2
Summer 2016 Mark Scheme

Ques	Solution	Mark	Notes
1(a)	$E(W) = 6$ $E(X^2) = \text{Var}(X) + [E(X)]^2 = 6$ $E(Y^2) = \text{Var}(Y) + [E(Y)]^2 = 12$ $\text{Var}(W) = E(X^2)E(Y^2) - [E(X)E(Y)]^2$ $= 36$	B1 M1A1 A1 M1A1	
(b)	<p>The possibilities are (1,4); (2,2); (4,1) si</p> $\text{Pr} = 2e^{-2} \times \frac{3^4}{4!} e^{-3} + \frac{2^2}{2!} e^{-2} \times \frac{3^2}{2!} e^{-3} + \frac{2^4}{4!} e^{-2} \times 3e^{-3}$ $= 0.12$	B1 M1A1 A1	Award the M1 for multiplying and adding Poisson probabilities. Accept use of tables
2(a)	$\bar{x} = \frac{637.2}{10} = 63.7(2)$ $\text{SE of } \bar{x} = \frac{1.9}{\sqrt{10}} \quad (0.6008\dots)$ <p>95% confidence interval limits are $63.7(2) \pm 1.96 \times 0.6008\dots$ giving [62.5, 64.9]</p>	B1 M1A1 M1A1 A1	M0 no working
(b)	<p>Width of 95% CI = $2 \times 1.96 \times \frac{1.9}{\sqrt{n}} = 1$</p> $n = 55.47\dots$ <p>Minimum $n = 56$ cao</p>	 M1A1 A1 A1	FT their z from (a)
3(a)	Upper quartile = $40 + 0.674(5) \times 2.5$ $= 41.7$	M1 A1	M0 no working
(b)(i)	<p>Let X=weight of a male, Y=weight of a female Let $U = X_1 + X_2 + X_3 + Y_1 + Y_2$ $E(U) = 3 \times 40 + 2 \times 32 = 184$ $\text{Var}(U) = 3 \times 2.5^2 + 2 \times 1.5^2 = 23.25$ $z = \frac{185 - 184}{\sqrt{23.25}} = 0.21$ Prob = 0.4168</p>	 B1 B1 M1A1 A1	Accept 0.417
(ii)	<p>Let $W = X_1 + X_2 + X_3 - 2(Y_1 + Y_2)$ $E(W) = 3 \times 40 - 4 \times 32 = -8$ $\text{Var}(W) = 3 \times 2.5^2 + 8 \times 1.5^2 = 36.75$ $z = \frac{8}{\sqrt{36.75}} = 1.32$ Prob = 0.9066</p>	 M1 A1 M1A1 m1A1 A1	Accept 0.907

Ques	Solution	Mark	Notes
4(a)	Under H_0 , $E(\bar{X} - \bar{Y}) = 0$ $\text{Var}(\bar{X} - \bar{Y}) = \frac{1.5^2}{8} + \frac{2.5^2}{12} (= 0.802...) \quad (77/96)$ H_1 is accepted if $\frac{ \bar{X} - \bar{Y} }{\sqrt{0.802...}} > 1.645$ $ \bar{X} - \bar{Y} > 1.473$ So $k = 1.473$	B1 B1 M1A1 A1	Accept 1.47
(b)(i)	Now, $E(\bar{X} - \bar{Y}) = 0.5$ si H_0 is accepted if $ \bar{X} - \bar{Y} \leq 1.473$, ie $-1.473 \leq \bar{X} - \bar{Y} \leq 1.473$ $z_1 = \frac{1.473 - 0.5}{\sqrt{0.802}} = 1.09$ $z_2 = \frac{-1.473 - 0.5}{\sqrt{0.802}} = -2.20$ Required probability = $0.8621 - 0.0139$ = 0.848	B1 M1 A1 M1A1 A1	FT k and variance Accept 1.08
(ii)	Required probability = $0.8621 - 0.0139$ = 0.848 An appropriate comment, eg The test is unlikely to detect small differences. This is a very high error probability.	A1 m1 A1 B1	Accept 0.8599 – 0.0139 Accept 0.846 FT probabilities greater than 0.5
5(a)(i)	$H_0 : p = 0.7; H_1 : p < 0.7$	B1	
(ii)	Let X denote number of seeds which germinate. Under H_0 , X is $B(50, 0.7)$ si p -value = $P(X \leq 32)$ Let Y denote number of non-germinating seeds. Under H_0 , Y is $B(50, 0.3)$ si p -value = $P(Y \geq 18)$ = 0.2178 Insufficient evidence to reject the seed manufacturer's claim.	B1 B1 B1 M1 A1 B1	FT the p -value if > 0.05
(b)	Under H_0 , X is now $B(500, 0.7) \approx N(350, 105)$ si Test statistic = $\frac{329.5 - 350}{\sqrt{105}}$ = -2.00 p -value = 0.0227 or 0.0228 Strong evidence to conclude that the germination rate is less than 0.7	B1B1 M1A1 A1 A1 B1	B1 mean, B1 variance Award M1A0 for incorrect or no continuity correction but FT for following marks No cc, $z = -2.05$, $p = 0.0202$ Wrong cc, $z = -2.10$, $p = 0.0179$ FT the p -value if < 0.05

Ques	Solution	Mark	Notes
6(a)	$P(Y < 8) = P(X > 12)$ $= 0.8$	M1 A1	Award the M1 for stating that Y is uniform on $[0,10]$
(b)(i)	$Y = 20 - X$	B1	
(ii)	$P(XY > 64) = P[X(20 - X) > 64]$ $= P(X^2 - 20X + 64 < 0)$ The critical values are 4 and 16 OR $P[(X - 4)(X - 16)] < 0$ The required region is $X < 16$ Prob = 0.6	M1 A1 A1 A1 A1	
(c)	EITHER Prob density of X is $f(x) = 0.1$ ($10 < x < 20$) si $E(XY) = \int_{10}^{20} (20x - x^2) \times \frac{1}{10} dx$ $= \frac{1}{10} \left[10x^2 - \frac{x^3}{3} \right]_{10}^{20}$ $= 66.7 \quad (200/3)$ OR $E(XY) = 20E(X) - E(X^2)$ $E(X) = 15$ $E(X^2) = \text{Var}(X) + [E(X)]^2$ $= 100/12 + 225 \quad (700/3)$ $E(XY) = 66.7 \quad (200/3)$	B1 M1A1 A1 A1 (M1) (B1) (M1) (A1) (A1)	Limits may be left until the next line